

Size variation of fossil rodent populations

M. Freudenthal and G. Cuenca Bescos

Freudenthal, M. & G. Cuenca Bescos, Size variation of fossil rodent populations.
— Scripta Geol., 76: 1-28, 16 figs., Leiden, July 1984.

Pearson's coefficient of variation is in general not applicable in palaeontology, due to the heterogeneity of samples. The heterogeneity may be due to the mixing of two species, mixture of material from various biotopes, or from a relatively large time span. A new coefficient of variation is proposed, based on the range of the sample. This coefficient may be used to estimate the degree of variation of a sample, and to decide whether it is homogeneous. Its application is tested empirically on a large number of samples of cricetid molars from the European Tertiary.

M. Freudenthal, Rijksmuseum van Geologie en Mineralogie, Hooglandse Kerkgracht 17, Leiden, Netherlands; G. Cuenca Bescos, Departamento de Paleontología, Universidad de Zaragoza, Spain.

Introduction	1
Variation in fossil Cricetidae	4
Remarks on samples with a high coefficient of variation	8
Conclusions	11
Literature	27

Introduction

In palaeontology a frequently used coefficient of variation is the one mentioned by Simpson et al., 1960, and which is known as Pearson's coefficient of variation:

$$V = \frac{100 s}{\bar{x}},$$

in which s is the standard deviation of a population of measurements, and \bar{x} is the arithmetic mean of that population. According to these authors, values of V fluctuate generally between 4 and 10, with a mean between 5 and 6, as far as the teeth of mammals are concerned.

Application of the above-mentioned formula to populations of molars of fossil Cricetidae (Rodentia, Mammalia) led the present authors to the view that the values found for V may easily pass beyond the limits stated; values between 3 and 4 turned out to be common, and we hardly ever found values over 5. Possibly each taxonomic group has its own specific values of V , and comparisons between populations may only be made within the limits of such a homogeneous group.

One of the practical applications of a coefficient of variation could be, that a high value for V might indicate that a sample is not homogeneous, but that it is composed of material of more than one species. Unfortunately, Pearson's (= Simpson's) coefficient of variation cannot be used in this way because: 1) calculation of V requires that the sample be taken from a normal distribution, and a sample containing more than one species is certainly not distributed normally; 2) if in a heterogeneous sample two species are represented by more or less equal numbers, Simpson's coefficient might still give a useful result. If, however, a sample is composed of a large number of specimens belonging to one species and only very few specimens belonging to a second species, the contribution of the latter to the value of the standard deviation will be negligible. As a result, the value of $100 s/\bar{x}$ will not deviate from the normal and the sample will be considered to be homogeneous.

Consequently, if one wishes to use V to decide whether a sample contains two species, the frequency of each of these species must be known in advance. But, if it were known in advance, there would be no need for further testing. This is particularly relevant, since hardly distinguishable species found together in the same locality usually do show a large difference in frequency.

This means that Pearson's coefficient of variation is not a good measure to decide whether a palaeontological sample contains one or two species. The quantity to be used for such a coefficient should be free from any preceding conditions. Mein & Freudenthal (1971) hinted that the range might be a quantity that fulfills this requirement.

The range gives much importance to the extreme measurements of the sample. Mathematically this is a disadvantage, because these values are much influenced by chance; a solution would be to leave out the upper and lower extremes, or the upper and lower quantiles, but this would reduce the palaeontological usefulness of the method. The best results were obtained by a new coefficient proposed here:

$$V' = \frac{100 R}{M},$$

in which R is the range (the difference between maximum and minimum), and M is the mid-point between maximum and minimum.

The mid-point is used instead of the arithmetic mean for several reasons: The mid-point requires little computation, as it is the sum of the minimum and maximum values divided by 2. This means that it may be calculated from every publication stating the minimum and the maximum value of a sample. For the calculation of the mean all measurements should be available. Secondly, the

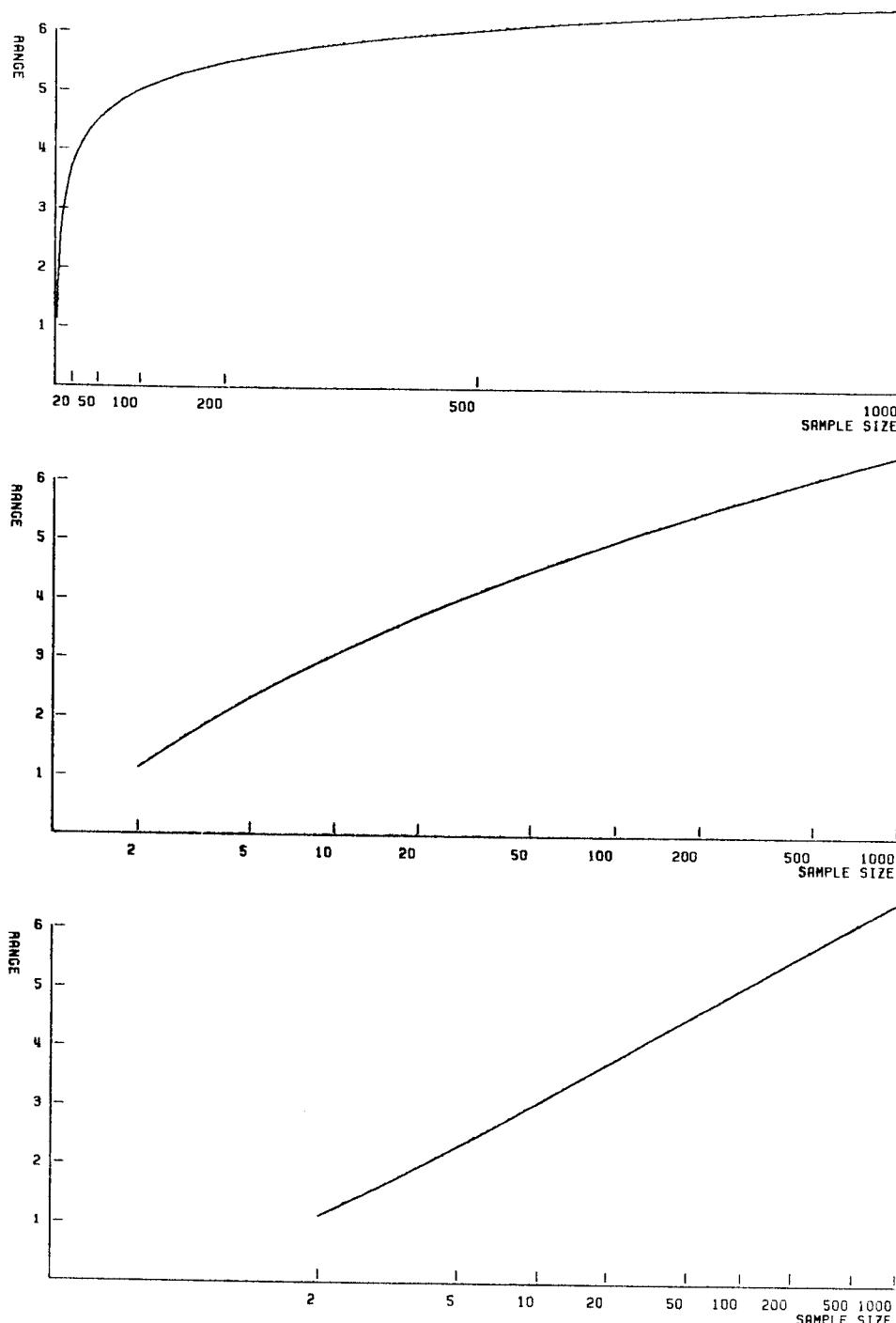


Fig. 1. Relation between range and sample size. The unit of the vertical axis is the standard deviation. The horizontal scale is linear in the upper graph, logarithmic in the middle one, and in the lower graph the scale is $\sqrt{\log N}$.

range is - mathematically - such an inaccurate value, that using the mean would give a false idea of precision. Thirdly, in a sample containing many specimens of a large species, and only a few specimens of a smaller species, V' would be too small if the mean were used.

Evidently, the range, and so the value of V' , is related to the number of specimens in the sample. The mean range, expressed in the standard deviation of the sample is a mathematical quantity known for samples taken from normal distributions. The relationship between the mean range and the sample size is given in Fig. 1. In the upper graph the scale of the horizontal axis (sample size) is linear. In the middle graph the scale is logarithmic, and in the lower graph the scale is the square root of the logarithm. In the latter case the relationship between the mean range and the sample size is practically linear, at least for values of N between 5 and 1000. In - palaeontological - practice values of N smaller than 5 are statistically not interesting, and values of N over 1000 are not found. It may be assumed that within the mentioned limits the relationship between V' and the square root of $\log N$ is linear too, provided that the samples be taken from normal distributions. Unfortunately, the latter condition is not necessarily fulfilled in palaeontological practice. Skew distributions appear not to be uncommon, and therefore results must be treated critically.

Variation in fossil Cricetidae

In order to get an idea of the distribution of V' for different values of N a number of about 140 populations were chosen, partly from the literature, partly from our own unpublished data, as specified in the following list. The figures preceding the items in the list refer to the publications cited in the chapter literature. Items without preceding figures are unpublished data, mainly from the research project 'Aragonian' which we are carrying out in collaboration with Dr R. Daams (Groningen University).

	Alcocer 2	<i>Megacricetodon crusafonti</i>
17	Anwil	<i>Cricetodon hagni</i>
17	Anwil	<i>Democricetodon brevis</i>
17	Anwil	<i>Democricetodon freisingensis</i>
17	Anwil	<i>Eumyaron latior</i>
17	Anwil	<i>Megacricetodon gregarius</i>
17	Anwil	<i>Megacricetodon minor</i>
17	Anwil	<i>Megacricetodon similis</i>
22	Armantes 1	<i>Fahlbuschia koenigswaldi</i>
22	Armantes 1	<i>Megacricetodon collongensis</i>
22, 23	Armantes 7	<i>Fahlbuschia larteti</i>
22	Arroyo del Val 6	<i>Fahlbuschia daricensis</i>
22	Arroyo del Val 6	<i>Megacricetodon crusafonti</i>
2	Beaumont 3	<i>Megacricetodon germanicus</i>
13	Bezian	<i>Megacricetodon bezianensis</i>
29	Bolgenachtal	<i>Eucricetodon praecursor</i>
	Borjas	<i>Megacricetodon crusafonti</i>
	Borjas	<i>Megacricetodon minor</i>

15	Buñol	<i>Democricetodon hispanicus</i>
15	Buñol	<i>Eumyarion valencianus</i>
15	Buñol	<i>Megacricetodon primitivus</i>
26	Can Llobateres	<i>Cotimus leemannii</i>
26	Can Llobateres	<i>Rotundomys sabadelliensis</i>
26, 35	Can Llobateres	<i>Ruscinomys thaleri</i>
35	Caravaca	<i>Ruscinomys lasallei</i>
	Carrilanga 1	<i>Megacricetodon debrijnii</i>
	Carrilanga 1	<i>Megacricetodon ibericus</i>
	Caseton 1 A	<i>Fahlbuschia</i> sp.
	Caseton 1 A	<i>Megacricetodon collongensis</i>
	Caseton 2 B	<i>Fahlbuschia</i> sp.
	Caseton 2 B	<i>Megacricetodon collongensis</i>
7	Castell de Barbera	<i>Democricetodon brevis</i>
14	Cetina de Aragon	<i>Eucricetodon gerandianus</i>
27	Coderet	<i>Eucricetodon thaleri</i>
27	Coderet C.1	<i>Adelomyarion vireti</i>
27	Coderet C.2	<i>Adelomyarion vireti</i>
27	Coderet C.3	<i>Eucricetodon collatus</i>
2	Collet-Redon	<i>Democricetodon mutilus</i>
2	Collet-Redon	<i>Megacricetodon bavaricus</i>
35	Concud 3	<i>Ruscinomys schaubi</i>
12	Cournon-les-Soumeroux	<i>Eucricetodon dubius</i>
11	Dieupentale	<i>Adelomyarion vireti</i>
11	Dieupentale	<i>Eucricetodon collatus</i>
21	Dorn-Dürkheim	<i>Democricetodon lavocati</i>
16	Eichkogel	<i>Kowalskia fahlbuschi</i>
20	Erkertshofen	<i>Democricetodon franconicus</i>
33	Escobosa de Calatañazor	<i>Cricetodon aguirrei</i>
33	Escobosa de Calatañazor	<i>Fahlbuschia larteti</i>
33	Escobosa de Calatañazor	<i>Megacricetodon crusafonti</i>
19	Giggenhausen	<i>Megacricetodon similis</i>
9	Heimersheim	<i>Eucricetodon moguntiacus</i>
19	Hesselohe	<i>Megacricetodon bavaricus</i>
32	Hoogbutsel	<i>Eucricetodon atavus</i>
4	Hostalets de Pierola	<i>Fahlbuschia crusafonti</i>
6	Hostalets de Pierola	<i>Hispanomys dispectus</i>
5	Hostalets de Pierola	<i>Megacricetodon ibericus</i>
19	Jettingen	<i>Megacricetodon gregarius</i>
27	Küttigen	<i>Eucricetodon collatus</i>
19	Langenmoosen	<i>Democricetodon gracilis</i>
19	Langenmoosen	<i>Democricetodon mutilus</i>
19	Langenmoosen	<i>Megacricetodon bavaricus</i>
22	Las Planas 4 A	<i>Megacricetodon collongensis</i>
22	Las Planas 4 A + 4 B	<i>Fahlbuschia daricensis</i>
22	Las Planas 4 A + 4 B	<i>Megacricetodon collongensis</i>
	Las Planas 4 C	<i>Megacricetodon collongensis</i>
	Las Planas 5 B	<i>Megacricetodon crusafonti</i>
	Las Planas 5 B	<i>Megacricetodon minor</i>
	Las Planas 5 H	<i>Megacricetodon crusafonti</i>
	Las Planas 5 L	<i>Megacricetodon crusafonti</i>
35	Layna	<i>Ruscinomys europaeus</i>
2	La Grenatière	<i>Fahlbuschia larteti</i>
2	La Grenatière	<i>Megacricetodon gregarius</i>

22	La Grive-St. Alban	<i>Democricetodon affinis</i>
22	La Grive-St. Alban	<i>Megacricetodon gregarius</i>
22	La Grive-St. Alban	<i>Megacricetodon minor</i>
22	La Romieu	<i>Democricetodon romieviensis</i>
22	La Romieu	<i>Megacricetodon collongensis</i>
23, 35	Los Mansuetos	<i>Ruscinomys schaubi</i>
2	Luc-sur-Orbieu	<i>Cricetodon sansaniensis</i>
2	Luc-sur Orbieu	<i>Democricetodon affinis</i>
2	Luc-sur Orbieu	<i>Megacricetodon crusafonti</i>
22, 23	Manchones	<i>Cricetodon jotae</i>
22	Manchones	<i>Fahlbuschia daricensis</i>
22	Manchones	<i>Megacricetodon crusafonti</i>
22	Manchones	<i>Megacricetodon minor</i>
35	Masada del Valle	<i>Hispanomys freudenthali</i>
23, 35	Masia del Barbo 2 A	<i>Hispanomys peralensis</i>
23, 35	Masia del Barbo 2 B	<i>Hispanomys peralensis</i>
2, 3	Montredon	<i>Hispanomys mediterraneus</i>
2, 3	Montredon N. Sup.	<i>Rotundomys montisrotundi</i>
1	Navarrete del Rio	<i>Eucricetodon aquitanicus</i>
23, 35	Nombrevilla	<i>Hispanomys nombrevillae</i>
25	Nombrevilla	<i>Megacricetodon debruijni</i>
25	Nombrevilla	<i>Megacricetodon ibericus</i>
	Olmo Redondo 1	<i>Democricetodon sp.</i>
	Olmo Redondo 2	<i>Democricetodon sp.</i>
	Olmo Redondo 5	<i>Megacricetodon primitivus</i>
	Olmo Redondo 8	<i>Megacricetodon primitivus</i>
	Olmo Redondo 9	<i>Megacricetodon primitivus</i>
25	Pedregueras 2 A	<i>Megacricetodon debruijni</i>
24	Pedregueras 2 C	<i>Democricetodon sulcatus</i>
23	Pedregueras 2 C	<i>Hispanomys aragonensis</i>
25	Pedregueras 2 C	<i>Megacricetodon debruijni</i>
24	Pedregueras 2 C	<i>Rotundomys hartenbergeri</i>
35	Peralejos C	<i>Hispanomys peralensis</i>
35	Peralejos D	<i>Hispanomys peralensis</i>
2	Port-la-Nouvelle	<i>Democricetodon mutilus</i>
2	Port-la-Nouvelle	<i>Megacricetodon collongensis</i>
8	Povoa de Santarem	<i>Fahlbuschia daricensis</i>
8	Povoa de Santarem	<i>Megacricetodon crusafonti</i>
36	Puttenhausen	<i>Democricetodon gracilis</i>
36	Puttenhausen	<i>Democricetodon mutilus</i>
36	Puttenhausen	<i>Eumyarion bifidus</i>
36	Puttenhausen	<i>Eumyarion weinfurteri</i>
36	Puttenhausen	<i>Megacricetodon germanicus</i>
19	Rosshaupten	<i>Megacricetodon gregarius</i>
19	Sandelzhausen	<i>Democricetodon gracilis</i>
19	Sandelzhausen	<i>Democricetodon mutilus</i>
22	Sansan	<i>Democricetodon brevis</i>
22	Sansan	<i>Democricetodon gailliardi</i>
10	Sansan	<i>Megacricetodon minor</i>
	San Roque 1	<i>Democricetodon sp.</i>
	San Roque 2	<i>Democricetodon sp.</i>
28	Saulzet	<i>Eucricetodon gerandianus</i>
	Solera	<i>Fahlbuschia sp.</i>
	Solera	<i>Megacricetodon crusafonti</i>

6	St. Quirze	<i>Cricetodon lavocati</i>
4	St. Quirze	<i>Fahlbuschia crusafonti</i>
22	Suevres	<i>Megacricetodon bourgeoisi</i>
	Toril 1	<i>Megacricetodon crusafonti</i>
	Toril 1	<i>Megacricetodon minor</i>
22	Torralba de Ribota	<i>Megacricetodon collongensis</i>
35	Tortajada A	<i>Hispanomys freudenthali</i>
7	Trinchera Nord Autopista	<i>Rotundomys bressanus</i>
	Valalto 1	<i>Megacricetodon crusafonti</i>
	Valalto 2 B	<i>Megacricetodon crusafonti</i>
	Valalto 2 C	<i>Megacricetodon crusafonti</i>
22	Valdemoros 1 A	<i>Fahlbuschia koenigswaldi</i>
22	Valdemoros 1 A	<i>Megacricetodon primitivus</i>
22	Valdemoros 3 B	<i>Fahlbuschia koenigswaldi</i>
22	Valdemoros 3 B	<i>Megacricetodon collongensis</i>
	Valdemoros 3 D	<i>Megacricetodon collongensis</i>
	Valdemoros 3 E	<i>Megacricetodon collongensis</i>
22	Valtorres	<i>Megacricetodon primitivus</i>
	Vargas 1 A	<i>Fahlbuschia sp.</i>
	Vargas 1 A	<i>Megacricetodon primitivus</i>
18	Vermes 1	<i>Democricetodon multilis</i>
31	Vieux-Collonges	<i>Cricetodon meini</i>
30	Vieux-Collonges	<i>Cricetodon sansaniensis</i>
	Vieux-Collonges	<i>Democricetodon affinis</i>
30	Vieux-Collonges	<i>Democricetodon affinis brevis</i>
	Vieux-Collonges	<i>Fahlbuschia sp.</i>
22	Vieux-Collonges	<i>Megacricetodon collongensis</i>
24	Villafeliche 2 A	<i>Democricetodon hispanicus</i>
22	Villafeliche 4	<i>Megacricetodon collongensis</i>
	Villafeliche 4 A	<i>Fahlbuschia sp.</i>
	Villafeliche 4 A	<i>Megacricetodon collongensis</i>
	Villafeliche 9	<i>Megacricetodon crusafonti</i>

Computation and the drawing of the graphs were carried out on the central computer of Leiden University, by means of a number of Fortran programs written by the first author. The full list of data and the computer programs are available upon request.

In the following M^1 stands for first upper molar, M_1 for first lower molar, and $M1$ for both upper and lower first molars. The same goes for M^2 and M^3 .

V' was calculated for each of the six elements of the dentition separately, and also for length and width separately. So each species from each locality may give a maximum of twelve figures for V' (figures based on less than five measurements were not used). For each of these twelve categories (length M_1 , width M_1 , length M^1 , width M^1 , length M^2 , etc.) a diagram was drawn, and these diagrams are given in Figs. 2 through 13.

On the horizontal axis V' is in a linear scale, the vertical axis is the logarithm of N (number of specimens in a sample). Each circle represents a sample of specimens of one element (e.g. M_1) of one species from one locality. If two or more of these circles overlap, one larger circle has been drawn. The size of the circle grows with the amount of overlapping values.

Obviously, V' is smallest in M_1 and M^1 , and largest in M^3 and M^2 . Also, V' is smaller for the lengths than for the widths (except in M^3 , where generally the

absolute value of the length is smaller than that of the width). Furthermore, the circles are more concentrated in the diagrams of M₁ and more scattered in M₃, and also more concentrated for the lengths, and more dispersed for the widths.

Partly this is due to a technical problem: it is easier to measure the length of a molar of a cricetid, than the width. Also, large and small teeth are measured with the same equipment, so, the measurement error must be relatively greater in a small tooth. But, even taking this into account, it seems that M₁ and M¹ are the least variable teeth of cricetids, and that M₃ and M³ vary most.

In all diagrams several points fall very much to the right, meaning that in these samples variation is extraordinarily high. These points were marked by the computer program that drew the diagrams, and represented by a letter or a cypher instead of a circle (in some cases these special characters are accompanied by an arrow, which means they actually should be farther to the right, outside the limit of the diagram). If a sample was marked special in one of the diagrams, it is represented by the same letter or cypher in the other diagrams too. In these other diagrams, however, it may fall well within the normal distribution of the circles.

Remarks on samples with a high coefficient of variation

- A) *Eucricetodon moguntiacus* from Heimersheim, published by Bahlo (1975). Bahlo states that it is difficult to separate this species from *E. atavus*, present in the same locality. Possibly his separation is not perfect.
- B) *Eucricetodon atavus* from Hoogbutsel published by Misonne (1957). The high coefficient of variability found in the width of M¹ is probably due to the small amount of material and the quality of the measurements. In a larger sample of (unpublished) material from this locality variability is normal.
- C) *Eucricetodon gerandianus* from Cetina de Aragon, published by Daams (1976). Variation in all elements but M₁ is normal. Inspection of an (unpublished) scatter diagram of the measurements of M₁ shows that possibly two different species are represented.
- D) *Eucricetodon gerandianus* from Saulcet, published by Hugueney (1974). Several elements have a rather high variation coefficient. A possible explanation might be that the material from Saulcet is in part from old collections, and in part newly collected. May be it does not originate from one single bed.
- E) *Adelomyarion vireti* from Coderet, published by Hugueney (1969), and from Dieupentale, published by Baudelot & Olivier (1978). In one of the populations from Coderet M¹ is rather variable in size. An explanation might be that *Adelomyarion* is not a cricetid, and that the so-called M¹ in reality is a mixture of P⁴ and DP⁴. This theory is supported by the fact that the number of specimens of M¹ is almost twice as high as the number of M₁. This theory does not account for the very high variability of the width of M₂. It agrees on the other hand with the highly variable morphology of M¹.

- F) *Hispanomys freudenthali* from Masada del Valle, published by van de Weerd (1976).
- G) *Hispanomys peralensis* from Masia del Barbo, published by van de Weerd (1976).
- H) *Hispanomys peralensis* from Peralejos C, published by van de Weerd (1976).
- I) *Hispanomys freudenthali* from Tortajada A, published by van de Weerd (1976).

Several elements of these four populations show rather high variability figures, with exceptionally high values for M³ from Masada del Valle and Masia del Barbo. Freudenthal (1966) noted a high variability for Masia del Barbo and expressed the opinion that two different species might be present, an opinion rejected by van de Weerd. The high values of variability found in *H. peralensis* and *H. freudenthali* may serve as an argument for a renewed study of this problem.

- J) *Cricetodon sansaniensis* from Vieux-Collonges, published by Mein (1958). This is a mixture of two species. Mein & Freudenthal (1971) recognized two species, *C. meini* and *C. aureus*, both having a normal variability.

K) *Democricetodon aff. brevis* from Vieux-Collonges, published by Mein (1958). This small population shows high values for several elements. A much larger (unpublished) population (about 100 specimens per element) from the same locality has about the same range of measurements; due to the larger amount of specimens the variability coefficient is normal. Consequently, the high values found in Mein's population may be considered to be accidental.

- L) *Democricetodon multilis* from Port-la-Nouvelle.
- M) *Democricetodon multilis* from Collet-Redon.
- N) *Megacricetodon gregarius* from La Grenatière.
- P) *Megacricetodon germanicus* from Beaumont 3.
- S) *Democricetodon affinis* from Luc-sur-Orbieu.

These five populations published by Aguilar (1980, 1981) show rather high variability values in some elements. A renewed study of this material might be worth-while.

- T) *Ruscinomys thaleri* from Can Llobateres, published by Hartenberger (1965). Variability is rather high, possibly due to the presence of two species.

- U) *Eumyaron bifidus* and *Eumyaron* cf. *weinfurteri* from Puttenhausen, published by Wu Wenyu (1982). The author states that variability in these species is very high. Our diagrams, however, show that this is not true.

- V) *Megacricetodon crusafonti* from Valalto 2 C (unpublished). Variability is high to very high in M1 and M2, more normal in M3. Quite probably two unseparable species (*crusafonti* and *minor* ?) are present. Like in many other cases (e.g. *Megacricetodon* from Armantes 7, Freudenthal, 1963, p. 92) the separation is first and best realized in M1, and the least in M3. Therefore, if a sample contains the first stage of separation of these two species, the M1 will give very high variability figures, whereas the values for M3 are quite normal.

W) *Megacricetodon crusafonti* from Las Planas 5 H (unpublished). Variability is somewhat high in several cases, probably due to the fact that the material contains a few specimens of *M. minor*.

X) *Megacricetodon collongensis* from Las Planas 4 C. Variability is rather high in the widths of M_1 and M^1 and the length of M_2 . There is no obvious reason to explain this.

Y) *Hispanomys nombrevillae* from Nombrevilla, published by Freudenthal (1966) and van de Weerd (1976). Some elements show a high variability on the basis of van de Weerd's data, low on the basis of Freudenthal's data. The figures given by these two authors differ considerably. Maybe the measurements should be reviewed.

Z) *Megacricetodon crusafonti* from Alcocer 2 (unpublished). Variability is quite high in some cases, possibly due to the presence of a few specimens of *M. minor*.

1) *Megacricetodon collongensis* and *Fahlbuschia darocensis* from Las Planas 4 A and 4 B, published by Freudenthal (1963), plus some unpublished new material. Both when Las Planas 4 A and 4 B are treated separately, and when they are taken together, variability in both mentioned species is quite high. The same goes for several other groups of rodents. A possible explanation is, that Las Planas 4 A and 4 B represent a stratigraphic level in which rather important faunal changes take place; that the fossiliferous bed represents a relatively large time span; that it contains - in part - reworked material; or that a considerable ecological change was taking place at the time of deposition (the locality is near the transition from one formation to another). In fact all these features may be causally related.

2) *Megacricetodon crusafonti* from Valalto 2 B (unpublished). The high variability in some elements may be due to the presence of a few specimens of *M. minor*.

3) *Ruscinomys europaeus* from Layna, published by van de Weerd (1976). M^2 shows a high variability. There is no obvious explanation.

4) *Democricetodon gracilis* from Puttenhausen, published by Wu Wenyu (1982). The variability of M_3 is very high, due to the presence of one extremely small specimen. Maybe this specimen belongs to a different species.

Table 1 lists the means and standard deviations of $v' / \sqrt{\log N}$. For the computation those data have been left out, that presented severe doubt as to their homogeneity.

Table 1. List of the means and standard deviations of $V'/\sqrt{\log N}$.

Element	Number of samples	Mean of $V'/\sqrt{\log N}$	standard deviation
length M ₁	126	13.48	3.22
width M ₁	126	15.30	3.90
length M ¹	118	13.38	3.38
width M ¹	118	15.18	3.62
length M ₂	124	13.03	3.60
width M ₂	124	14.55	3.77
length M ²	113	14.82	3.69
width M ²	113	15.15	3.66
length M ₃	96	16.24	4.12
width M ₃	99	15.77	4.76
length M ³	85	19.61	5.36
width M ³	85	16.51	5.12

Conclusions

The new coefficient of variation proposed in this paper appears to be a useful instrument to estimate variability of a sample. The value of V' appears to be dependent upon the type of material considered. It is not possible to give a general value for V' . For each group of related data the mean value of V' must be calculated separately, and conclusions may only be drawn if a sufficiently large number of comparable data is available. So far only for fossil cricetids such a number is available. We tried to apply the same method to glirids and sciurids, but for these groups the number of available data is not sufficient. Nevertheless we got the impression that for these groups the values differ considerably from those for cricetids.

Neither are the values we calculated for cricetids completely reliable. Our choice whether samples are homogeneous or heterogeneous is quite arbitrary. Future research may alter the results achieved in this paper.

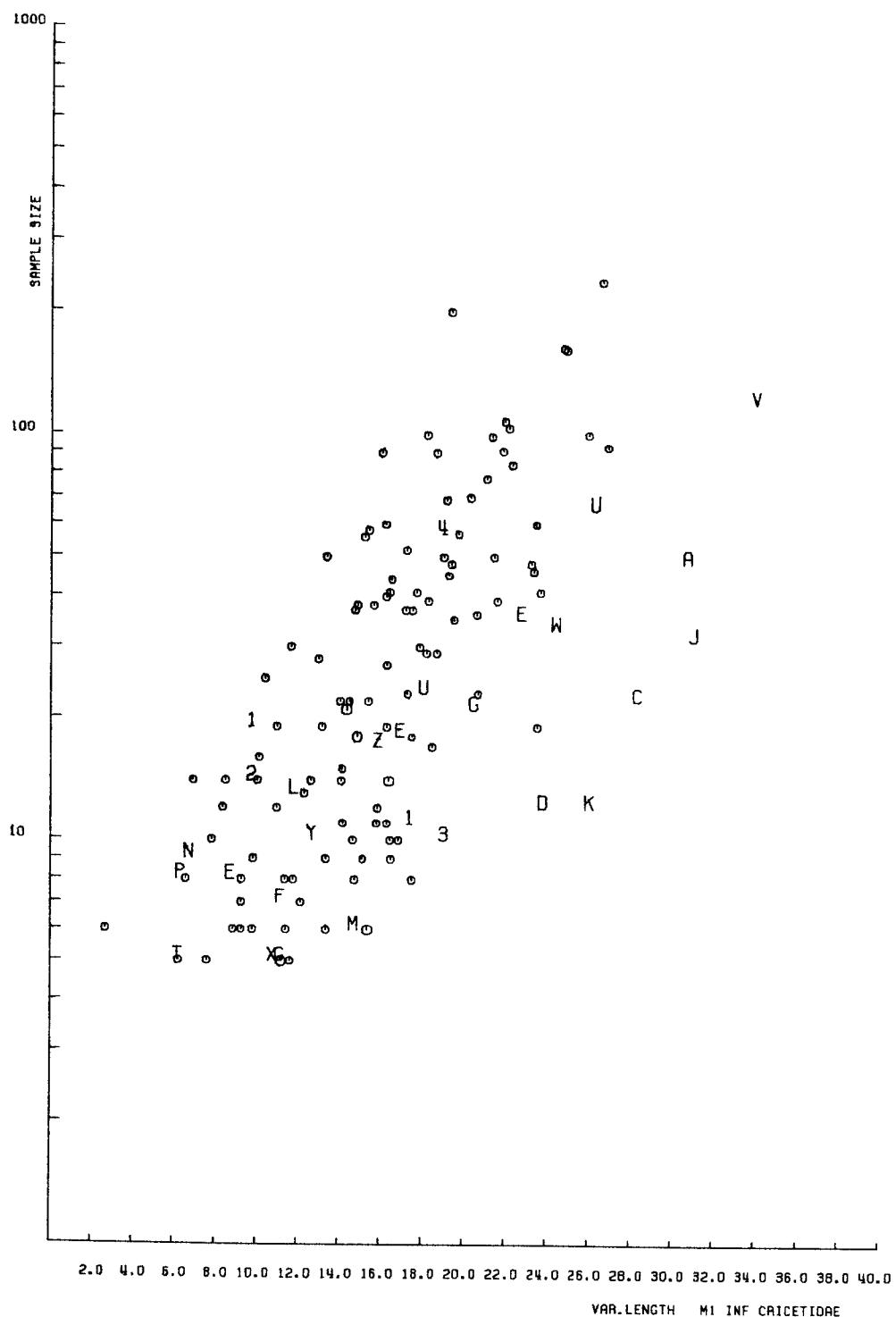


Fig. 2. Relation of V' and sample size for length of M_1 . Vertical scale is logarithmic.

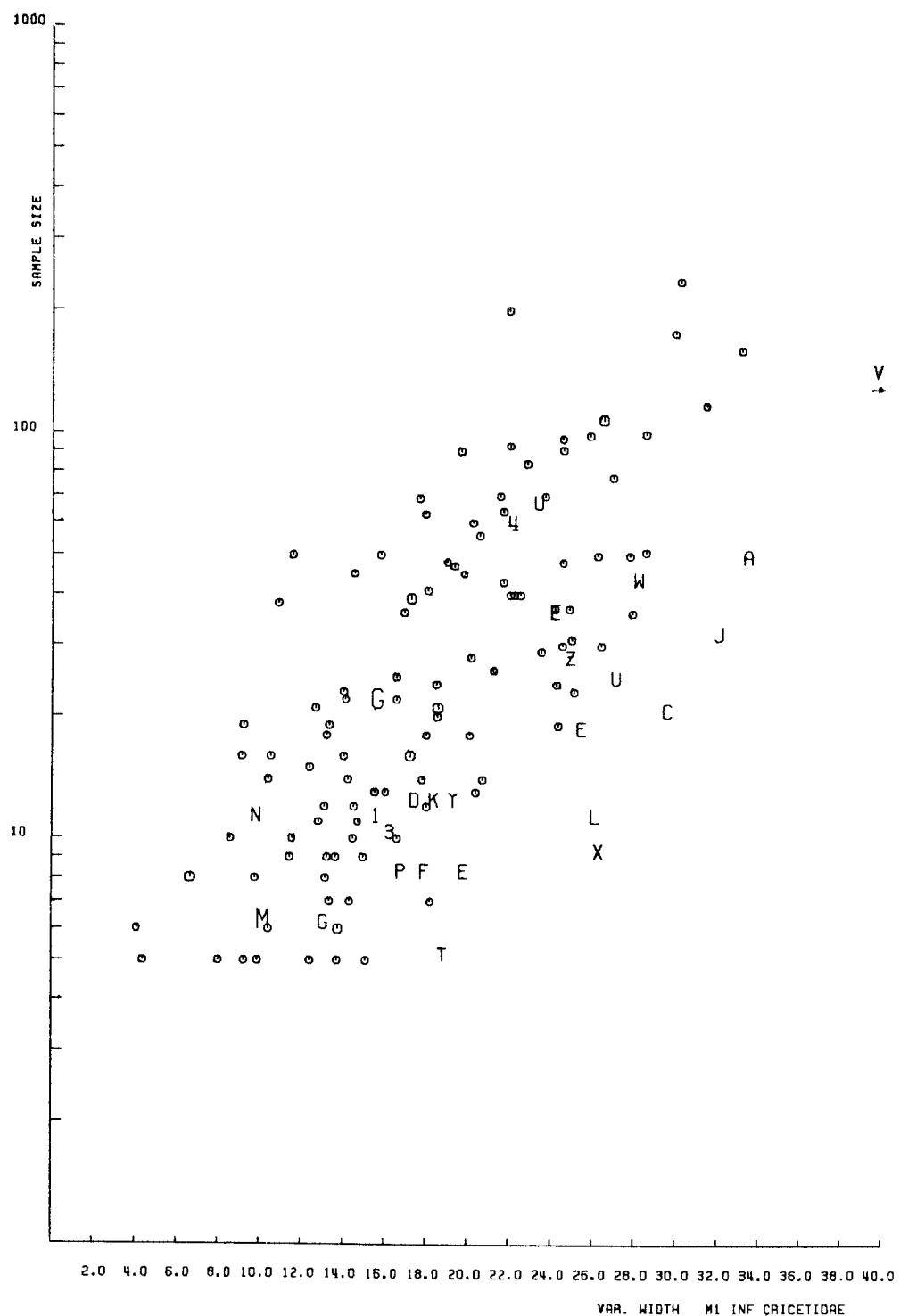


Fig. 3. Relation of V' and sample size for width of M_1 . Vertical scale is logarithmic.

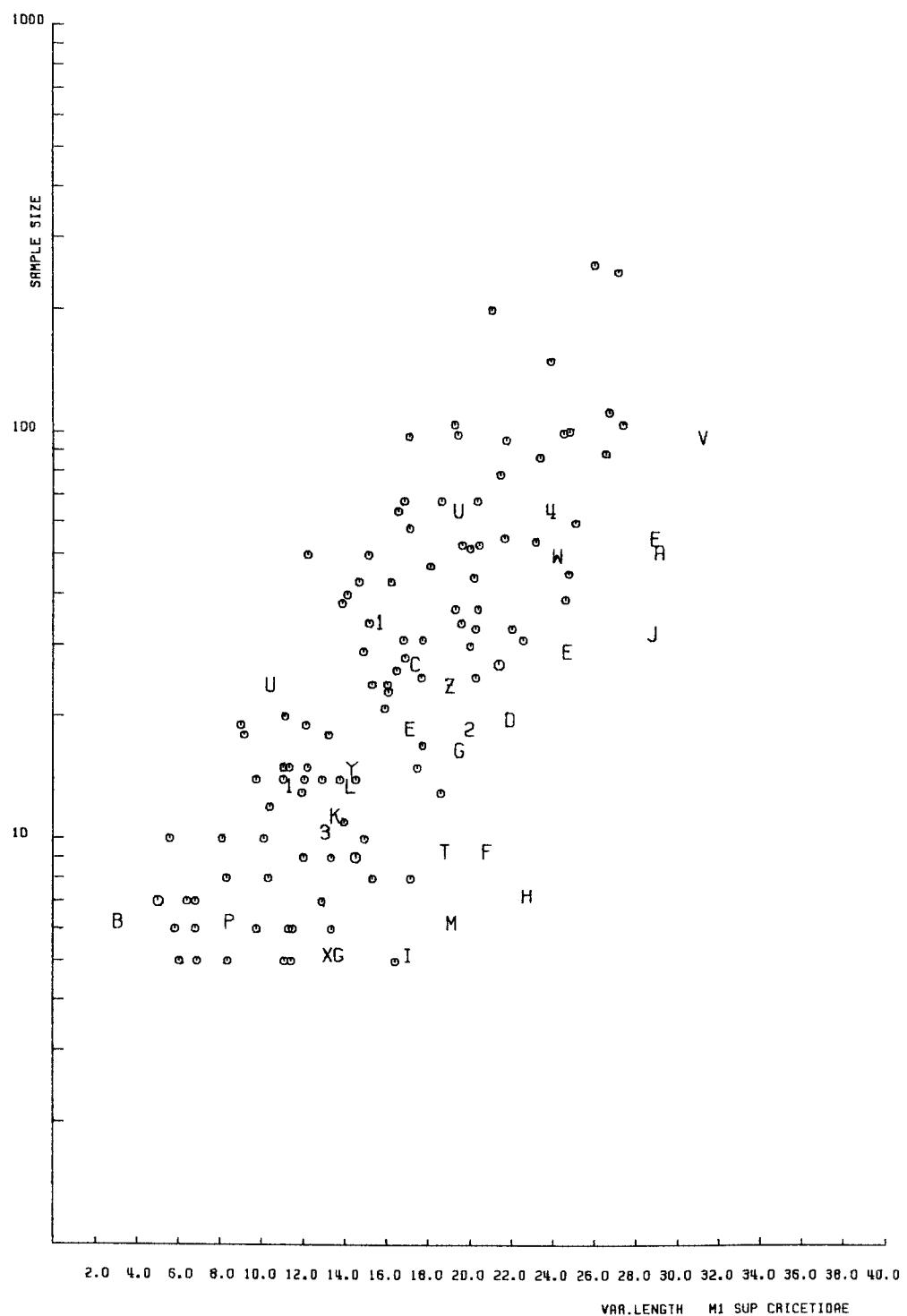


Fig. 4. Relation of V' and sample size for length of M^1 . Vertical scale is logarithmic.

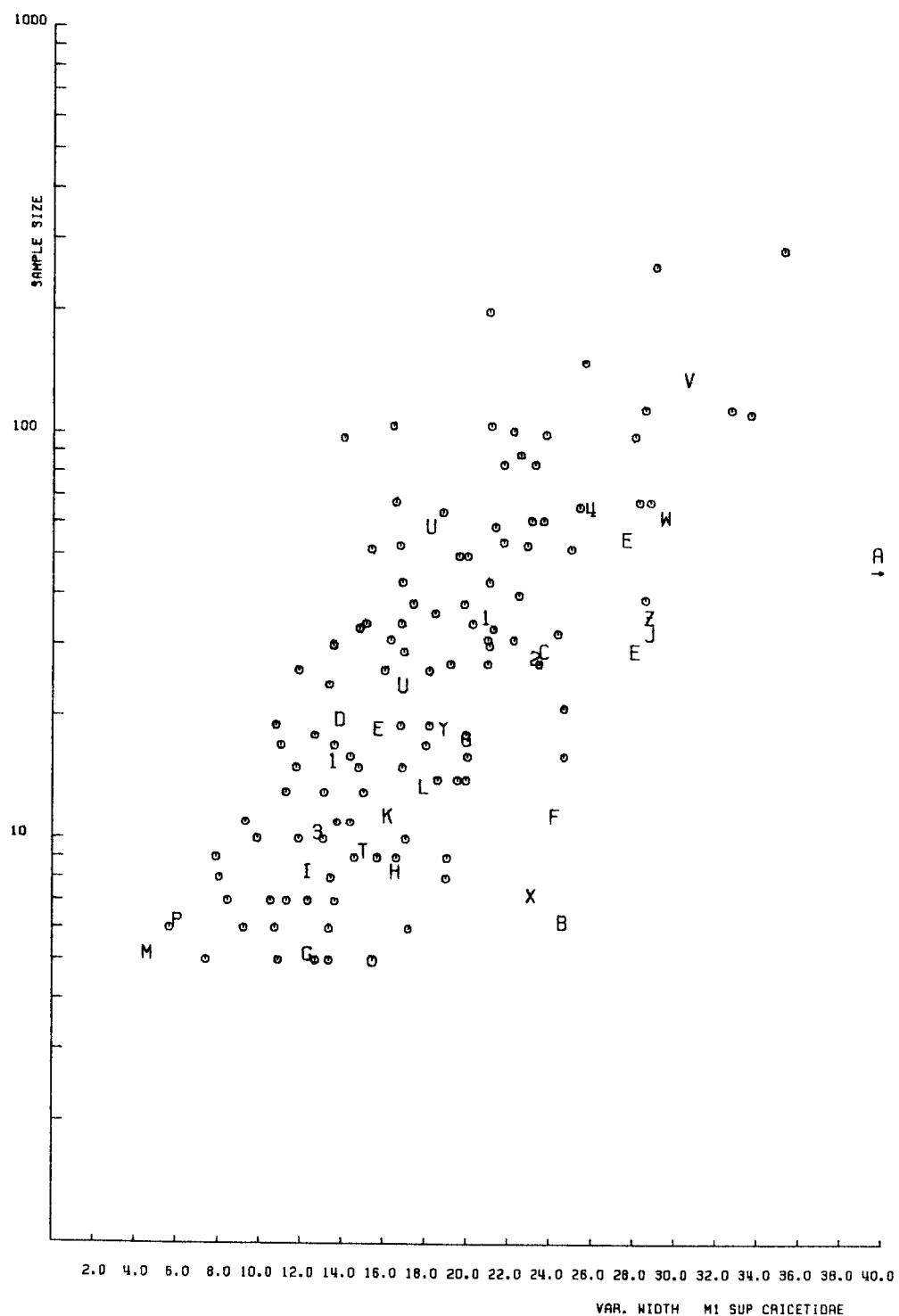


Fig. 5. Relation of V' and sample size for width of M^1 . Vertical scale is logarithmic.

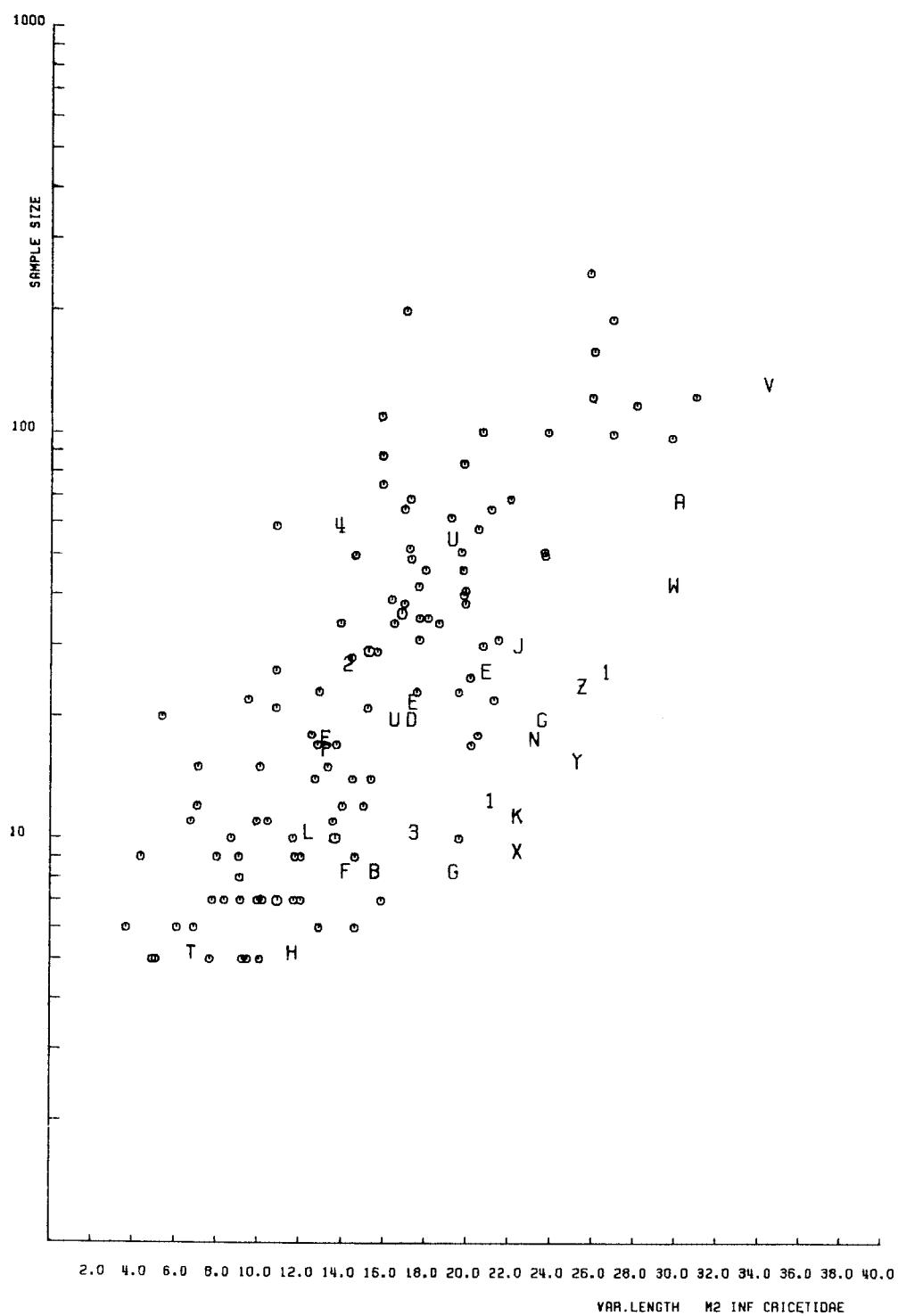


Fig. 6. Relation of V' and sample size for length of M_2 . Vertical scale is logarithmic.

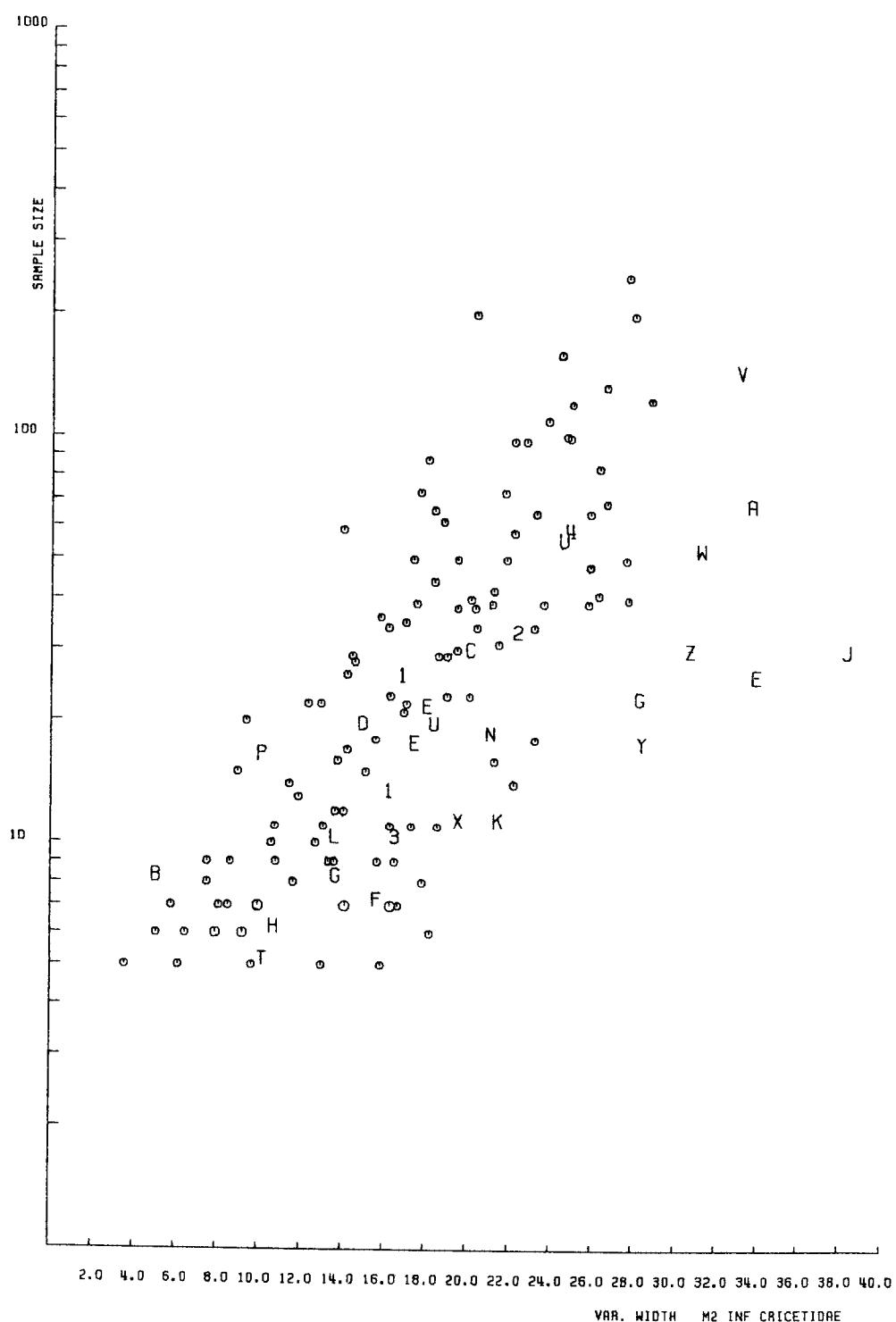


Fig. 7. Relation of V' and sample size for width of M₂. Vertical scale is logarithmic.

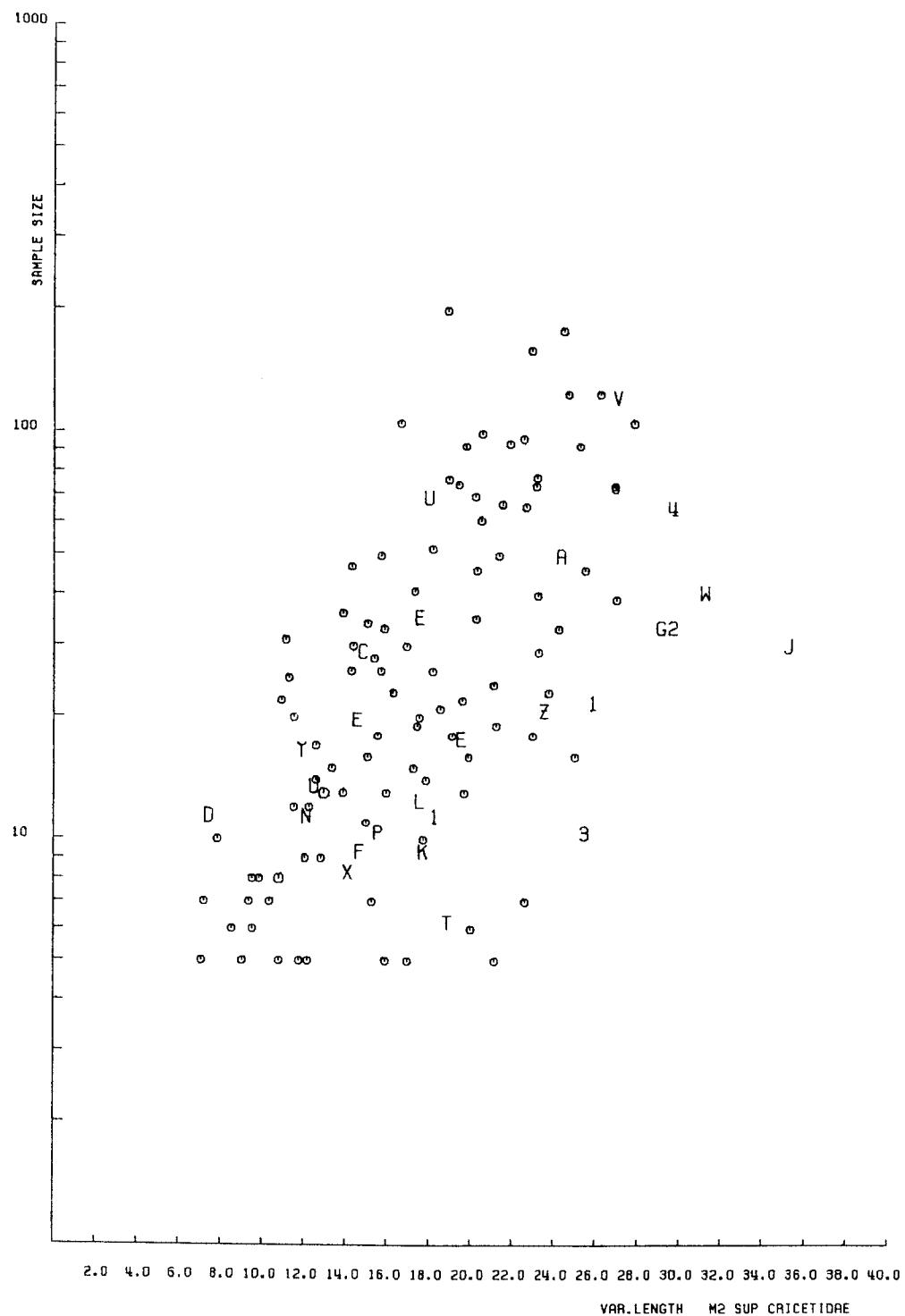


Fig. 8. Relation of V' and sample size for length of M^2 . Vertical scale is logarithmic.

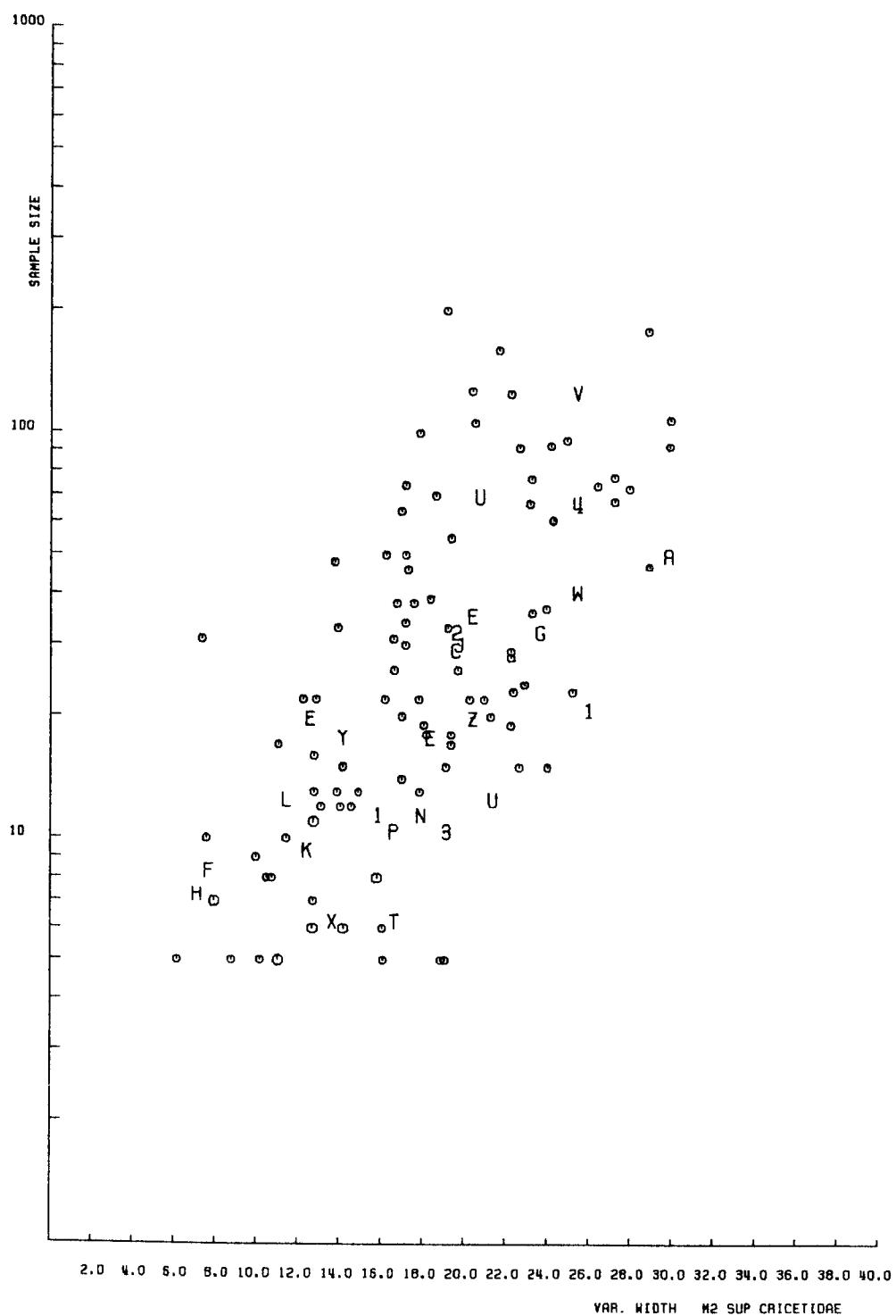


Fig. 9. Relation of V' and sample size for width of M². Vertical scale is logarithmic.

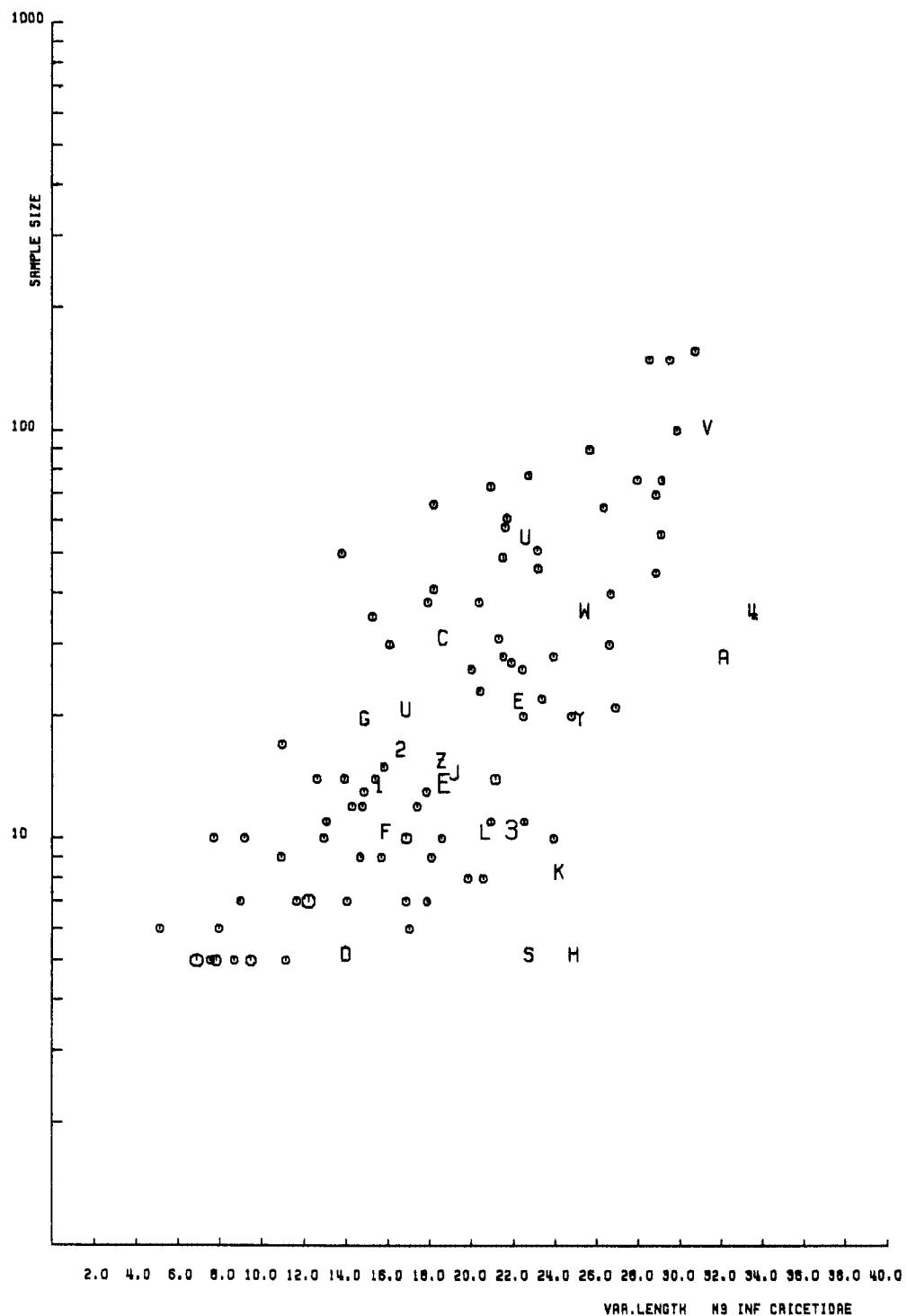


Fig. 10. Relation of V' and sample size for length of M_3 . Vertical scale is logarithmic.

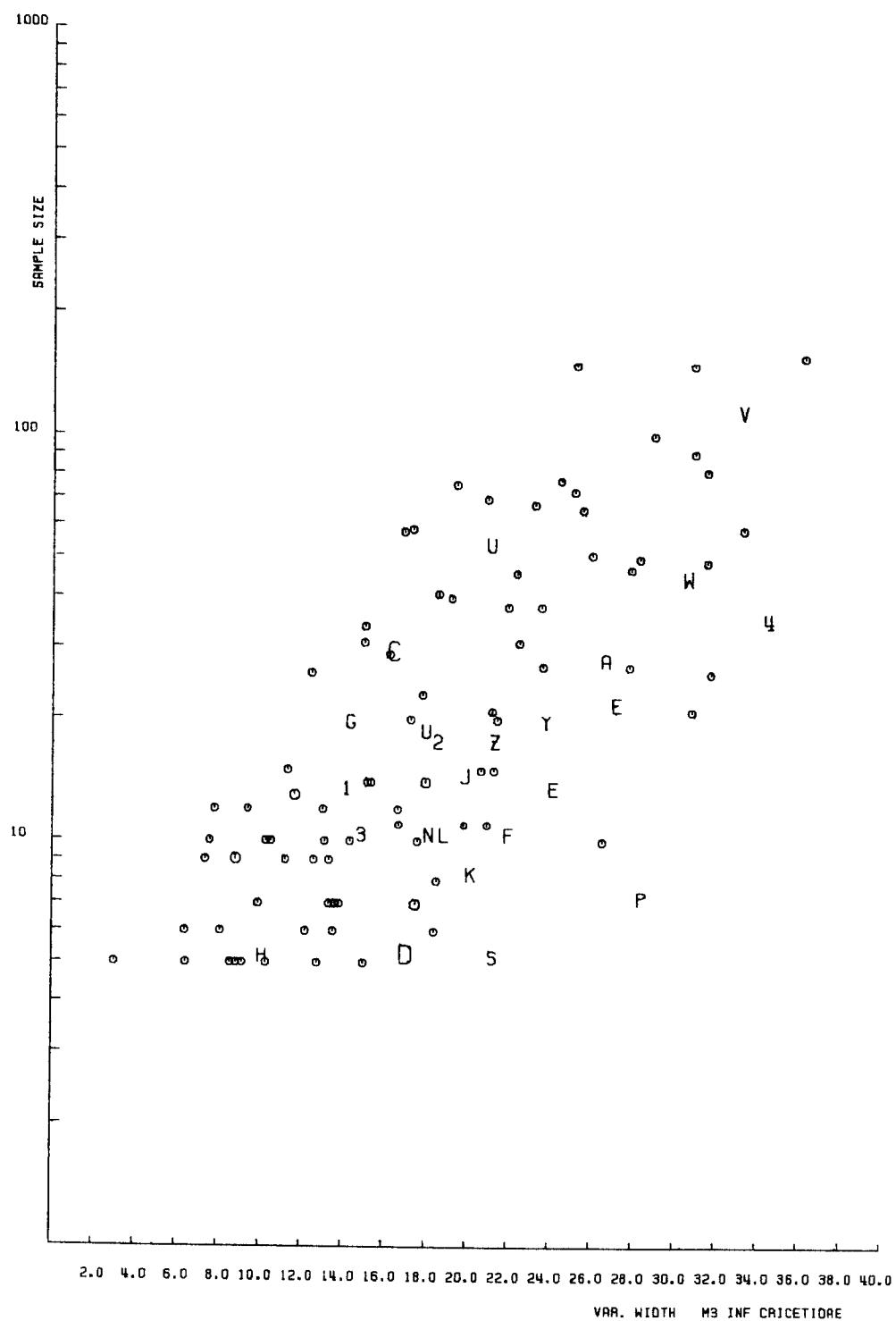


Fig. 11. Relation of V' and sample size for width of M₃. Vertical scale is logarithmic.

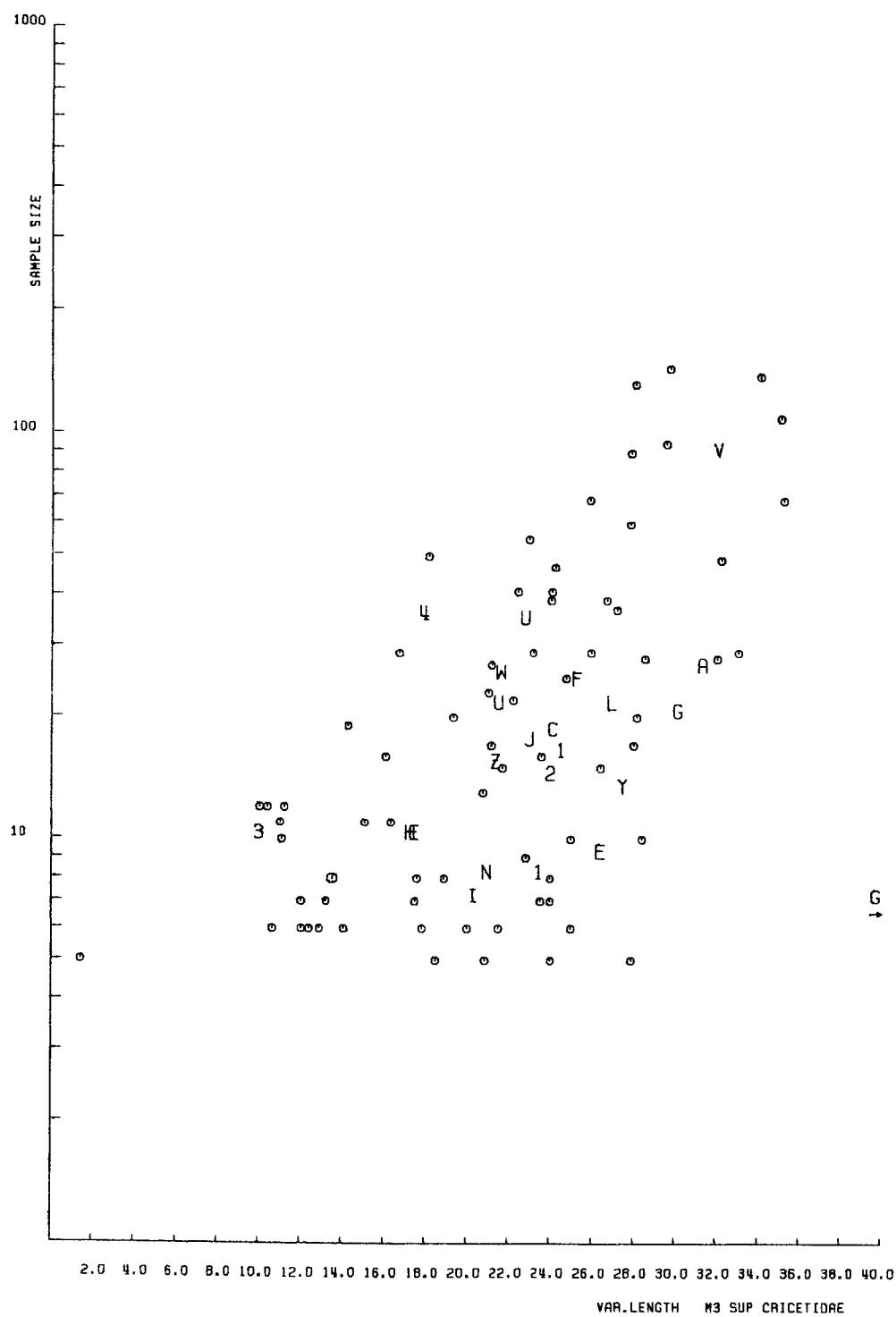


Fig. 12. Relation of V' and sample size for length of M^3 . Vertical scale is logarithmic.

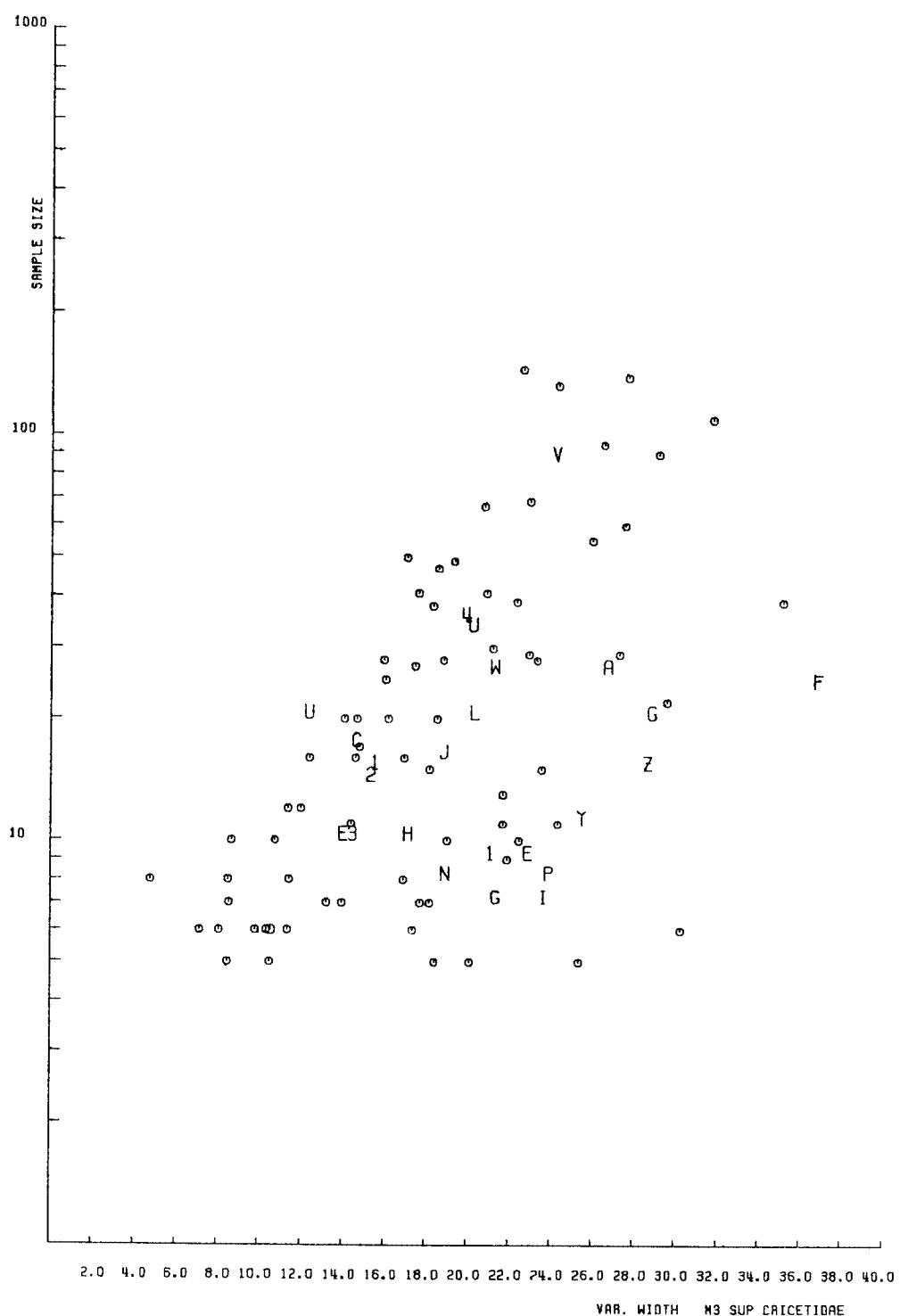


Fig. 13. Relation of V' and sample size for width of M_3 . Vertical scale is logarithmic.

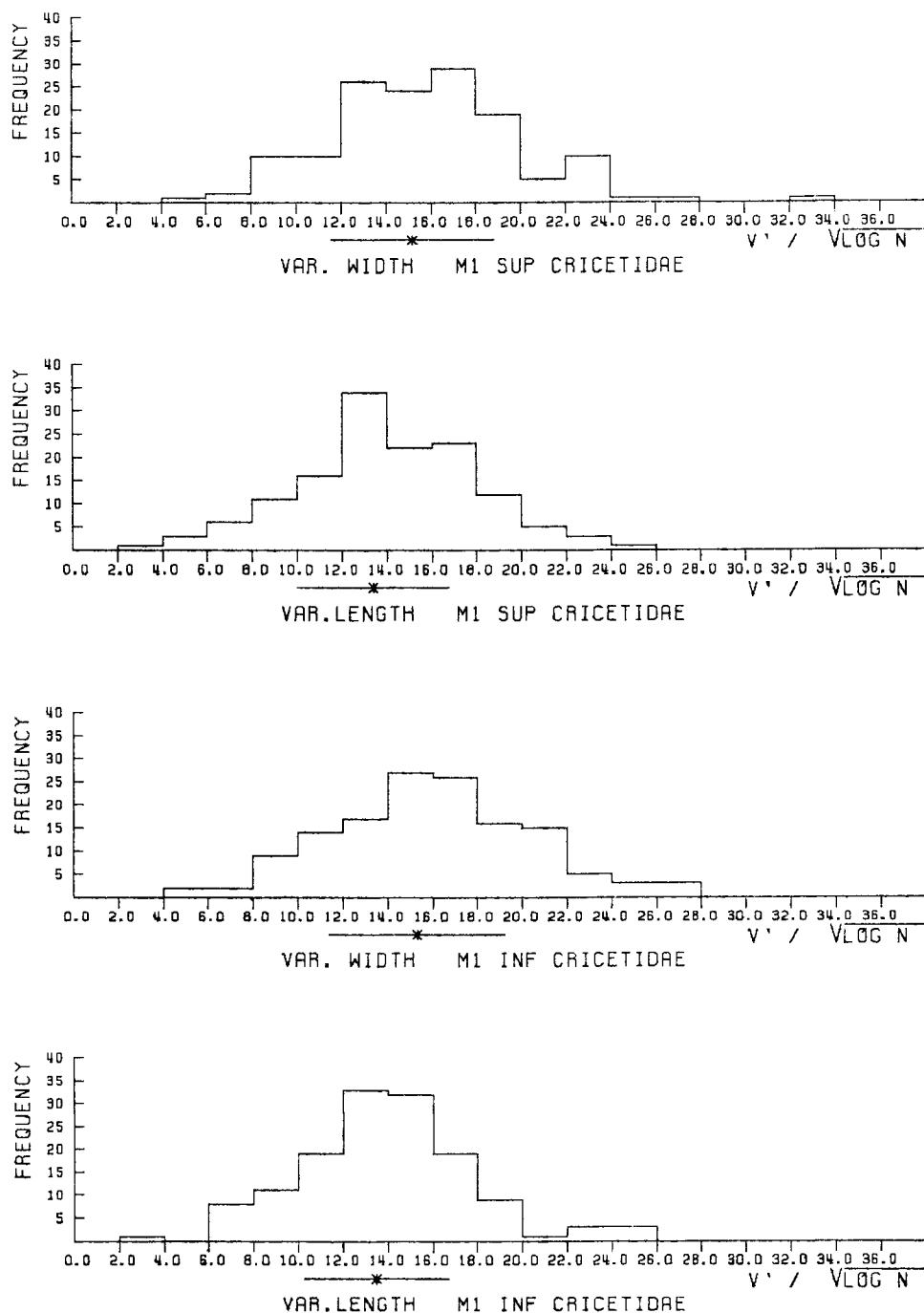


Fig. 14. Histograms of $V' / \sqrt{\log N}$ for the first molars of Cricetidae. The line under each histogram represents 2 standard deviations, the asterisk indicates the mean value.

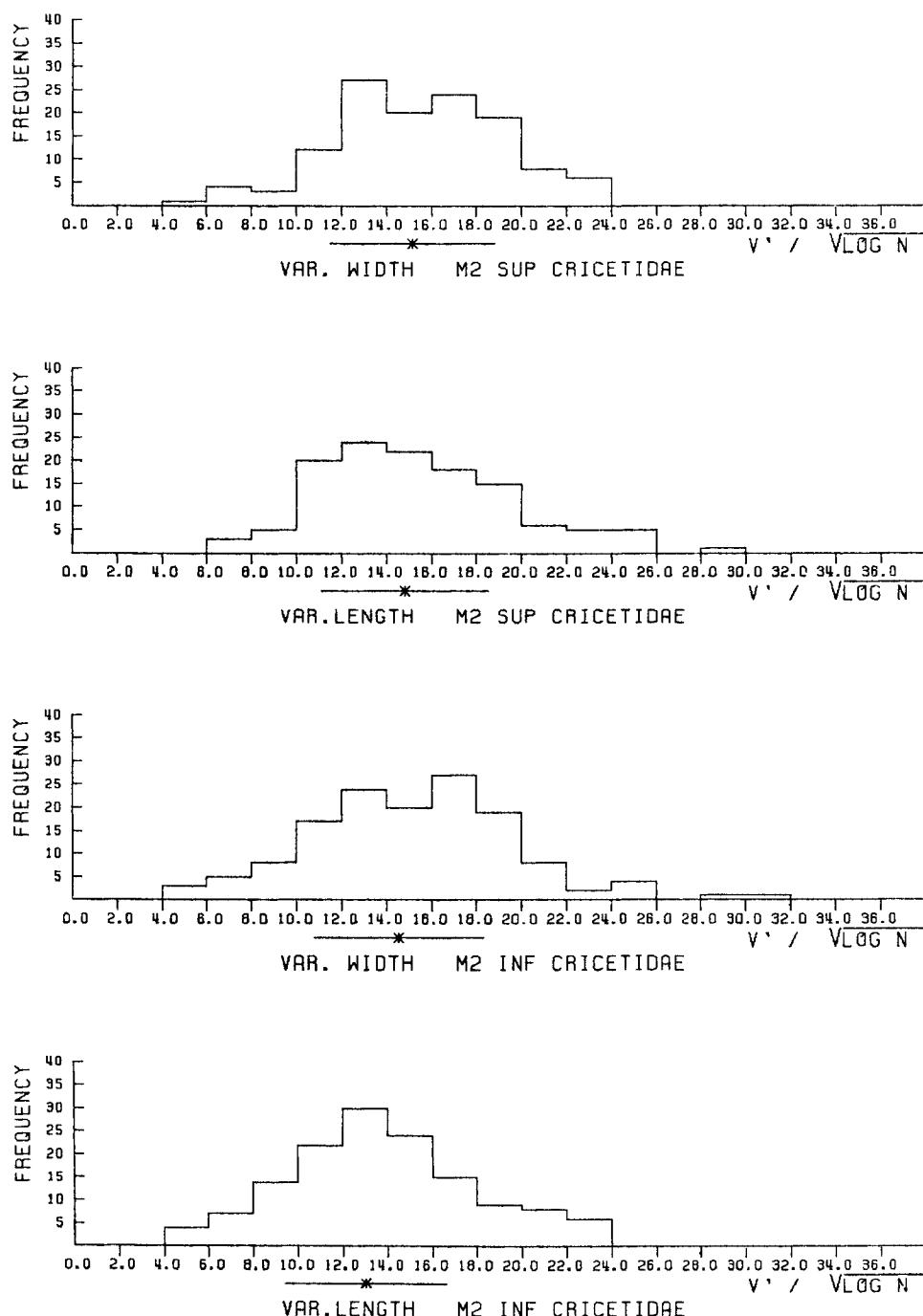


Fig. 15. Histograms of $V' / \sqrt{\log N}$ for the second molars of Cricetidae. The line under each histogram represents 2 standard deviations, the asterisk indicates the mean value.

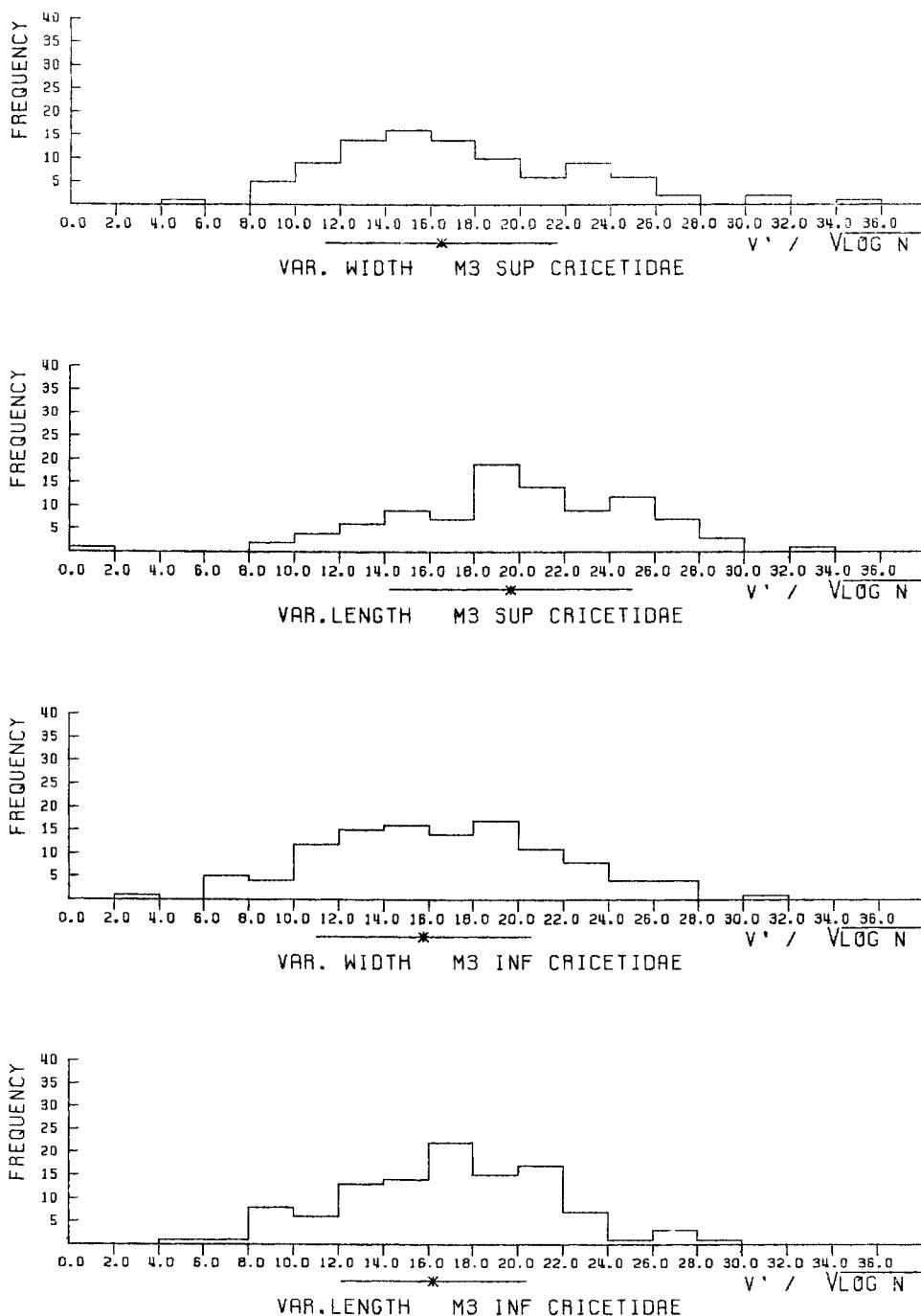


Fig. 16. Histograms of $V'/\sqrt{\log N}$ for the third molars of Cricetidae. The line under each histogram represents 2 standard deviations, the asterisk indicates the mean value.

Literature

The numbers preceding the titles refer to the list of material used.

- (1) Adrover, R., 1978. Les rongeurs et lagomorphes (Mammalia) du Miocène inférieur continental de Navarrete del Rio (Province de Teruel, Espagne). – Docum. Lab. Géol. Fac. Sci. Lyon, 72: 3-47, 5 pls.
- (2) Aguilar, J.P., 1981. Evolution des rongeurs miocènes et paléogéographie de la Méditerranée occidentale. – Doctor's thesis Univ. Montpellier: 203 pp., 5 pls.
- (3) Aguilar, J.P., 1982. Contributions à l'étude des micromammifères du gisement Miocène supérieur de Montredon (Hérault). 2. Les rongeurs. – Palaeovertebrata, 12, 3: 81-117.
- (4) Agusti, J., 1978. *Fahlbuschia crusafonti* nov. sp., cricétido nuevo del Astaraciense superior del Vallés-Penedés. – Inst. Paleont. Sabadell, 1, 2: 63-68.
- (5) Agusti, J., 1980. Sobre *Megacricetodon ibericus* (Schaub) (Rodentia, Mammalia) de Hostalets de Pierola (Vallés-Penedés). – But. Inf. Inst. Paleont. Sabadell, 12, 1-2: 35-39.
- (6) Agusti, J., 1980. La asociación de *Hispanomys* y *Cricetodon* (Rodentia, Mammalia) en el Mioceno superior del Vallés-Penedés (Cataluña, España). – Acta Geol. Hisp., 15, 2: 51-60.
- (7) Agusti, J., 1980. Roedores miomorfos del Neógeno de Cataluña. – Doctor's thesis Univ. Barcelona.
- (8) Antunes, M.T. & P. Mein, 1977. Contribution à la paléontologie du Miocène moyen continental du Bassin du Tage. 3. Mammifères. Póvoa de Santarém, Pero Filho et Chões (Secorio). Conclusions générales. – Ciências da Terra (UNL). Lisboa, 3: 143-165.
- (9) Bahlo, E., 1975. Die Nagetiersauna von Heimersheim bei Alzey (Rheinhessen, West-deutschland) aus dem Grenzbereich Mittel/Oberoligozän und ihre stratigrafische Stellung. – Abh. Hess. Landesamt Bodenf., 71: 1-182.
- (10) Baudelot, S., 1972. Etude des chiroptères, insectivores et rongeurs du Miocène de Sanson (Gers). – Doctor's thesis Univ. Toulouse, 496: 1-364, 16 pls.
- (11) Baudelot, S. & P. Olivier, 1978. Les rongeurs (Mammalia, Rodentia) de l'Oligocène terminal de Dieupentale (Sud-Ouest de la France: Tarn-et-Garonne). – Geobios, 11, 1: 5-19.
- (12) Brunet, M., M. Hugueney & Y. Jehenne, 1981. Cournon-les-Soumeroux, un nouveau site à vertébrés d'Auvergne, sa place parmi les faunes de l'Oligocène supérieur d'Europe. – Geobios, 14, 3: 323-359.
- (13) Bulot, C., 1972. Les Cricetidae (Rodentia) de Bézian (Gers). – Bull. Soc. Hist. nat. Toulouse, 108, 3-4: 349-356.
- (14) Daams, R., 1976. Miocene rodents (Mammalia) from Cetina de Aragon (prov. Zaragoza) and Buñol (prov. Valencia), Spain. – Proc. Kon. Acad. Wet., B, 77, 3: 201-240.
- (15) Daams, R. & M. Freudenthal, 1974. Early Miocene Cricetidae (Rodentia, Mammalia) from Buñol (Valencia, Spain). – Scripta Geol., 24: 1-19, 2 pls.
- (16) Daxner-Hock, G., 1972. Cricetinae aus dem Alt-Pliozän von Eichkogel bei Mödling (Niederösterreich) und von Vösendorf bei Wien. – Paläont. Z., 46, 3/4: 133-150.
- (17) Engesser, B., 1972. Die obermiozäne Säugetierfauna von Anwil (Baselland). – Tätigkeitsber. Naturf. Ges. Baselland, 28: 35-363, 6 pls.
- (18) Engesser, B., A. Matter & M. Weidmann, 1981. Stratigraphie und Säugetierfaunen des mittleren Miozäns von Vermes (Kt. Jura). – Eclogae Geol. Helvetiae, 74, 3: 893-952.
- (19) Fahlbusch, V., 1964. Die Cricetiden (Mammalia) der Oberen Süßwassermolasse Bayerns. – Abh. Bayer. Akad. Wiss., 118: 1-136, 7 pls.

- (20) Fahlbusch, V., 1966. Cricetidae (Rodentia, Mammalia) aus der mittelmiozänen Spaltenfüllung Erkertshofen bei Eichstätt. – Mitt. Bayer. Staatssamml. Paläont. hist. Geol., 6: 109-131, 1 pl.
- (21) Franzen, J.L. & G. Storch, 1975. Die unterpliozäne (turolische) Wirbeltierfauna von Dorn-Dürkheim, Rheinhessen (SW-Deutschland). 1. Entdeckung, Geologie, Mammalia: Carnivora, Proboscidea, Rodentia. – Senckenbergiana Lethaea, 56, 4/5: 233-303.
- (22) Freudenthal, M., 1963. Entwicklungsstufen der miozänen Cricetodontinae (Mammalia, Rodentia) Mittelspaniens und ihre stratigrafische Bedeutung. – Beaufortia, 10, 119: 51-157, 1 pl.
- (23) Freudenthal, M., 1966. On the mammalian fauna of the Hipparium-beds in Calatayud-Teruel Basin (prov. Zaragoza, Spain). Part 1: The genera *Cricetodon* and *Ruscinomys* (Rodentia). – Proc. Kon. Akad. Wet., B, 69, 2: 296-317, 2 pls.
- (24) Freudenthal, M., 1967. On the mammalian fauna of the Hipparium-beds in the Calatayud-Teruel Basin (prov. Zaragoza, Spain). Part 3: *Democricetodon* and *Rotundomys* (Rodentia). – Proc. Kon. Akad. Wet., B, 70, 3: 298-315, 2 pls.
- (25) Freudenthal, M., 1968. On the mammalian fauna of the Hipparium-beds in the Calatayud-Teruel Basin (prov. Zaragoza, Spain). Part 4: The genus *Megacricetodon* – Proc. Kon. Akad. Wet., B, 71, 1: 57-72, 1 pl.
- (26) Hartenberger, J.L., 1966. Les Cricetidae (Rodentia) de Can Llobateres (Neogène d'Espagne). – Bull. Soc. Géol. France, 7, 7: 487-508, 1 pl.
- (27) Hugueney, M., 1969. Les rongeurs (Mammalia) de l'Oligocène supérieur de Coderet-Branssat (Allier). – Doc. Lab. Géol. Fac. Sci. Lyon, 34: 1-227, 5 pls.
- (28) Hugueney, M., 1974. Gisements de petits mammifères dans la région de Saint-Gérand-le-Puy (stratigraphie relative). – Revue Sci. Bourbonnais, 1974: 52-68.
- (29) Hünerman, K.A. & H. Sulser, 1981. Die Cricetodontinen (Mammalia, Rodentia) aus der Unterer Süßwassermolasse des Bolgenachtals (Österreich, Vorarlberg). – Eclogae Geol. Helvetiae, 74, 3: 865-881.
- (30) Mein, P., 1958. Les mammifères de la faune sidérolithique de Vieux-Collonges. – Nouv. Arch. Mus. Hist. Nat. Lyon, 5: 1-122.
- (31) Mein, P. & M. Freudenthal, 1971. Les Cricetidae (Mammalia, Rodentia) du Néogène moyen de Vieux-Collonges. Partie 1. Le genre *Cricetodon* Lartet, 1851. – Scripta Geol., 5: 1-51, 6 pls.
- (32) Misonne, X., 1957. – Mammifères Oligocènes de Hoogbutsel et Hoeleden. – Bull. Inst. R. Sci. nat. Belg., 33, 51: 1-15, 2 pls.
- (33) Sesé, C., 1977. Los cricetidos (Rodentia, Mammalia) de las fisuras del Miocene medio de Escobosa de Calatañazor (Soria, España). – Trab. Neog./Quatern., 8: 127-180.
- (34) Simpson, G.C., A. Roe & R.C. Lewontin, 1960. Quantitative zoology. – Harcourt, Brace & World, New York: 1-440.
- (35) Weerd, A. van de, 1976. Rodent faunas of the Mio-Pliocene continental sediments of the Teruel-Alfambra region, Spain. – Utrecht Micropal. Bull., Spec. Publ., 2: 1-217, 16 pls.
- (36) Wu Wenyu, 1982. Die Cricetiden (Mammalia, Rodentia) aus der Oberen Süßwassermolasse von Puttenhausen (Niederbayern). – Zitteliana, 9: 37-80, 3 pls.